

Juliet balconies using BALCONY 2 System (Aerofoil) handrail with reinforcing bar

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<u>Structural Calculations for Juliet balconies using BALCONY 2 System (Aerofoil) handrail with 58 x 4mm internal reinforcing bar</u>

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Juliet balconies using BALCONY 2 System (Aerofoil) handrail

DESIGN TO EUROCODES & CURRENT BRITISH STANDARDS

Dacion	standards:
Design	stanuarus.

EN 1990 Eurocode 0: Basis of structural design. EN 1991 Eurocode 1: Actions on structures. EN 1993 Eurocode 3: Design of steel structures. EN 1999 Eurocode 9: Design of aluminium structures. BS EN 1990:2002 + A1:2005 Eurocode: UK National annex for Eurocode BS 6180:2011 British standard: Barriers in and about buildings. BS EN 1991-1-1-4:2005 + A1 2010 Eurocode 1 Wind actions on structures

<u>Design loads:</u> Occupancy class/es for

which this design applies

(Table 2: BS6180:2011)

Domestic and residential activities (i) & (ii)

Office and work areas not included elsewhere (iii), (iv) & (v)

Areas without obstacles for moving people and not susceptible to

overcrowding (viii) & (ix)

Service load on handrail Q_k

0.74 kN/m uniformly distributed line load acting 1100mm above finished floor level. (Table 2: BS6180:2011)

above missied most level. (Table 2. 550100.2

Service load applied to the glass infill

 Q_{k1} = A uniformly distributed load of 1.0 kN/m²

Point load on glass infill

= 0.50 kN applied to any part of the glass fill panels.



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Table 2 Minimum horizontal imposed loads for parapets, barriers and balustrades

Type of occupancy for part of the building or structure	Examples of specific use	Horizontal uniformly distributed line load	Uniformly distributed load applied to the infill	A point load applied to part of the infill	
		(kN/m)	(kN/m ²)	(kN)	
Domestic and residential activities	All areas within or serving exclusively one single family dwelling including stairs, landings, etc. but excluding external balconies and edges of roofs	0.36	0.5	0.25	
	(ii) Other residential, i.e. houses of multiple occupancy and balconies, including Juliette balconies and edges of roofs in single family dwellings	0.74	1.0	0.5	
Offices and work areas not included	(iii) Light access stairs and gangways not more than 600 mm wide	0.22	-	_	
elsewhere, including storage areas	(iv) Light pedestrian traffic routes in industrial and storage buildings except designated escape routes	0.36	0.5	0.25	
	(v) Areas not susceptile to overcrowding in office and institutional buildings, also industrial and storage buildings except as given above	0.74	1.0	0.5	
Areas where people might congregate	(vi) Areas having fixed seating within 530 mm of the barrier, balustrade or parapet	1.5	1.5	1.5	
Areas with tables or fixed seatings	(vii) Restaurants and bars	1.5	1.5	1.5	
Areas without obstacles for	(viii) Stairs, landings, corridors, ramps	0.74	1.0	0.5	
moving people and not susceptible to overcrowding	(ix) External balconies including Juliette balconies and edges of roofs. Footways and pavements within building curtilage adjacent to basement/sunken areas	0.74	1.0	0.5	

@ BSI 2011 • 9

Table 2: BS6180:2011

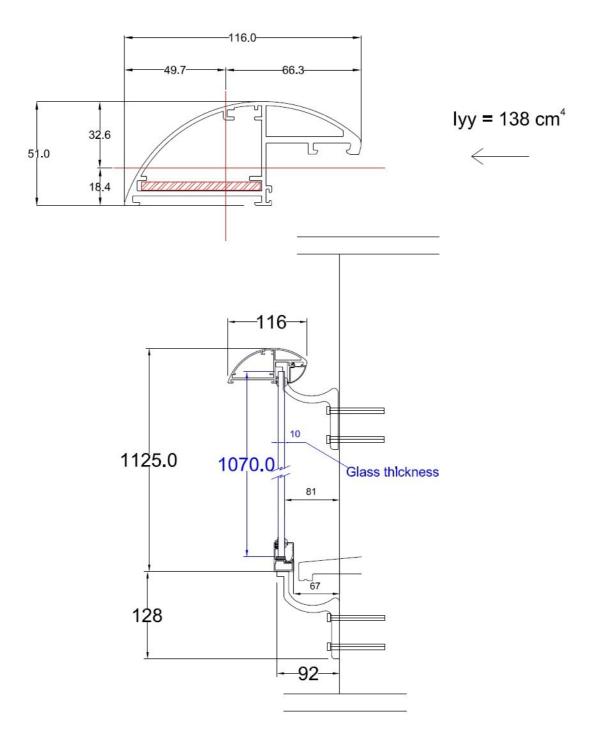
- These imposed loads are considered as three separate load cases. They are not combined.
- Factored loads are used for checking the limit state of static strength of a member.
- The service loads are multiplied by a partial factor for variable action $\gamma_{Q,1}$ of 1.5 to give the ultimate design load for leading variable action.

Deflection:

- All structural members deflect to some extent under load. Service loads are used to calculate deflections.
- The total displacement of any point of a barrier from its original unloaded position under the action of service loads is limited to 25mm.



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Typical section & handrail profile moment of inertia



PAGE 4 (ref: JULB2WB130417)

Balcony 2 system: Section properties of handrail with internal reinforcing bar:

Material type	=	Extruded alum	ninium type 6063	T5
Characteristic 0.2% proof stress	=	f_{\circ}	=	130 N/mm ²
Characteristic ultimate tensile strength	=	f_{u}	=	175 N/mm ²
Modulus of elasticity	=	E	=	70 000 N/mm ²
Shear modulus	=	G	=	27 000 N/mm ²
Moment of inertia about the y-y axis	=	I yy	=	138 cm ⁴
about the y y axis				
Least elastic modulus about the y-y axis	=	W_{el}	=	22.908 cm ³
Partial factor for material properties	=	ү м1	=	1.10
Value of shape factor	=	α	=	W_{pl}/W_{el}
(conservative value)		u	=	1.2 say
Design ultimate resistance				
to bending about the y-y axis	=	M_{Rd}	=	$M_{o,Rd}$
	=	$lpha$ W _{el} $f_{ m o}$ / $\gamma_{ m M1}$		
	=	1.2 x 22.908 c	m³ x 130 N/mm²	<u>x (10)⁻³</u>
		2 240 lables	1.1	
	=	3.249 kNm		



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0.74 kN/m x 1.5 Design ultimate horizontal F load on handrail 1.11 kN/m $F L^2$ Design horizontal moment M on handrail between points of support. Allowable span L between points $[8 \times M_{Rd}]^{0.5}$ of support based upon the moment [8 x 3.249 kNm]^{0.5} capacity of the handrail 1.11 4.839m say = 4.80m

In terms of bending capacity the handrail can span up to 4.8m simply supported between points of support. However the maximum standard length of handrail used is 4.1m. Service load deflection is limited to 25mm.

The support brackets at each end of the handrail are 80mm wide. For a 4100mm long handrail the span centre to centre of the support brackets is 4020mm.

Deflection (Δ) of span (L) $\Delta = \frac{5 \text{ F L}^4}{384 \text{ E I}}$ for an imposed UDL (F) 384 E I For a handrail 4.1m long with the span c/c support brackets 4.02m $\Delta = \frac{5 (740 \times 4.02) (4020)^3}{384 \times 70 \ 000 \times 138 \times (10)^4}$ = 26.05mm = slightly > than 25mm but say OK

Therefore deflection limitations govern the allowable span of the handrail between points of support in respect of the horizontal imposed service uniformly distributed line load.

In order to comply with service load deflection limitations the allowable span of the handrail is limited to **4.02 metres** between the centres of supporting brackets.

Handrail brackets:

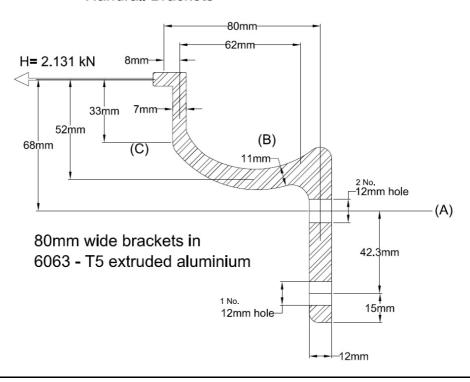
The horizontal imposed design load on the handrail can only act over the clear width of the opening, ie. 3840mm for a handrail 4100mm long overall. The bracket design load H is calculated for a maximum loaded length equal to the maximum clear opening width.

For the maximum clear opening width of 3840mm:



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Handrail Brackets



Bracket section (A)											
Factored applied moment	M	=	2.131 kN x 0.068								
		=	0.144 kNm								
Limiting stress in bending	f_o	=	130 N/mm ²								
Moment capacity of section	M_{c}	=	130 N/mm ² x 2016 mm ³ x (10) ⁻⁶								
			1.1								
		=	0.238 kNm > 0.144 kNm OK								
Section (B)											
Dimensions at section (B)		=	80 mm wide x 11mm thick								
Factored applied moment	М	=	2.131 kN x 0.052								
• •		=	0.111 kNm								
Plastic section modulus	W_{pl}	=	80 x (11) ²								
			4								
		=	2420 mm ³								
Moment capacity of section	M_c	=	130 N/mm ² x 2420 mm ³ x (10) -6								
·			1.1								
		=	0.286 kNm > 0.111 kNm OK								



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Handrail brackets:

Section (C)

Dimensions of section		=	80 mm wide x 7mm thick
Factored applied moment	M	= =	2.131 kN x 0.033 0.070 kNm
Plastic section modulus	W_{pl}	=	$\frac{80 \times (7)^2}{4}$
		=	980 mm ³
Moment capacity of section	M_{c}	=	130 N/mm ² x 980 mm ³ x (10) -6
			1.1
		=	0.116 kNm > 0.070 kNm OK
Shear force at section (C)	V	=	2.131 kN
Design plastic shear resistance	$V_{pl,RD}$	=	$A_{v}(f_{v}/\sqrt{3})$

The handrail brackets are adequate to resist the ultimate design bending and shear forces in respect of the maximum handrail span of 4.02 metres between bracket centres.

Handrail bracket fixing bolt forces:

(2 No. M10 bolts top; 1 No. M10 bolt bottom of bracket).

(80 x 7) (190 / 1.732) x (10) -3 1.0

>

2.131 kN

OK

ү мо

61.43 kN

Moments taken about the lower bolt for the direct pull-out force on the top 2 No. bolts:

Consider the maximum span c/c brackets of 4.02 m (loaded length of handrail 3.84 m)

Factored load on bracket	Н	=	2.131 kN		
Direct tension on top 2 bolts	Т	=	2.131 x 0.110	=	5.54 kN
			0.0423		
		=	2.78 kN/bolt	(ultimate load)	
		=	1.85 kN/bolt	(working load)	

BS 6180:2011, section 6.5, recommends that barrier fixings, attachments and anchorages should be designed to withstand a greater load than the design loading for the barrier generally. This is intended to ensure that under an extreme load condition, barriers show indications of distress by distortion, before there is any possibility of sudden collapse due to failure of the fixings. A 50% increase in the design load on fixings is recommended.

Applying the above recommendation, the **ultimate** direct pull-out force on the upper bolts becomes $2.78 \times 1.5 = 4.17$ **kN/bolt**. The **working** load pull-out force on the upper bolts becomes $1.85 \times 1.5 = 2.78 \times$

The nominal tension capacity of M10 (8.8 grade) bolts is greater than these design forces. The allowable load is therefore determined by the pull-out resistance of the drilled resin anchor bolts or similar, and also by the strength of the structure into which they are installed to support these loads, and not by the tension capacity of the bolts themselves.



PAGE 8 (ref: JULB2WB130417)

Handrail brackets: working loads on fixing bolts:

For shorter standard length handrails the pull-out forces on bracket fixing bolts are proportionally lower.

Handrail length	opening size	working load tension on each upper bolt (including 50% increase recommended in BS 6180)
1280mm	1020mm	0.74 kN
1500mm	1240mm	0.90 kN
1680mm	1420mm	1.03 kN
1860mm	1600mm	1.16 kN
2180mm	1920mm	1.39 kN
2450mm	2190mm	1.58 kN
2840mm	2580mm	1.86 kN
3200mm	2940mm	2.12 kN

Lower rail brackets: These brackets have the same sectional profile as the handrail brackets but are 40mm wide rather than 80mm. 1 No. 12mm diameter hole is provided top and bottom for M10 bolts, making the effective width of the vertical leg 28mm. The section modulus and moment capacity of the brackets is therefore half that of the handrail brackets. The brackets are installed at 500mm nominal maximum centres. The brackets support the dead load from the glass and rails.

Dead load from glass + rails		=	0.26 kN/m x 1.35 (γ)		=	0.351 kN/m factored	
Factored vertical load per bracket at 500mm centres.		=	0.351 / 2		=	0.176 kN/bracket	
Factored moments:							
Section (A)	M	=	0.176 kN x 0.08	=	0.0141	. kNm	
	M_c	=	0.238 kNm / 2	=	0.119	kNm	OK
Section (B)	М	=	0.176 kN x 0.07	=	0.0123	kNm	
	M_c	=	0.286 kNm / 2	=	0.143	kNm	OK
Section (C)	M	=	0.176 kN x 0.008	=	0.0014	kNm	
	M_c	=	0.116 kNm / 2	=	0.058	kNm	OK

The brackets are adequate to resist the design factored moments.

<u>Bolt loads:</u> (1 No. 10mm diameter bolt top and bottom of bracket)

Direct tension on top bolt T = $0.176 \text{ kN} \times 0.086$ = 0.36 kN (factored load) = 0.0423

Applying the 50% increase in fixing loads recommended in BS 6180, this becomes **0.54 kN/bolt** (ultimate load) and **0.36 kN/bolt** (working load).

Shear force: on 2 No. bolts = $\frac{0.176 \text{ kN}}{2}$ = 0.09 kN/bolt say

Applying the 50% increase as per BS 6180, this becomes **0.135 kN/bolt (ultimate load)** and **0.09 kN/bolt (working load)**.



PAGE 9 (ref: JULB2WB130417)

Glass infill:

Design standard Institution of Structural Engineers publication Structural use of glass

in building (second edition) February 2014.

10mm thermally toughened soda silicate safety glass with smooth Glass type

'as produced' finish with polished edges.

120 N/mm² Characteristic design strength

Ultimate design stress $f_{g;d}$ K_{mod} x K_{sp} x K_{g;k} $Kv (f_{b;k} - f_{g;k})$ $\gamma_{M;A}$ **ү**м;v

 K_{mod} where: 30 second load duration factor

0.89 for a domestic balustrade load

glass surface profile factor K_{sp} 1.0 for float glass 'as produced' =

characteristic strength of basic annealed glass $f_{g;k}$

45 N/mm²

manufacturing process strengthening factor Κ_ν =

1.0 for horizontal toughening

characteristic strength of processed glass $f_{b:k}$

> 120 N/mm² =

= material partial factor **γ** м;А

1.6 for basic annealed glass

material partial factor V M;V =

> 1.2 for surface prestressed (toughened) glass =

Ultimate design stress $f_{g;d}$ 0.89 x 1.0 x 45 1.0(120 - 45)

1.6 1.2

87.53 N/mm² =

Section modulus of glass Ζ $1000 \times (10)^2$ 16667 mm³/m 6

10mm thick

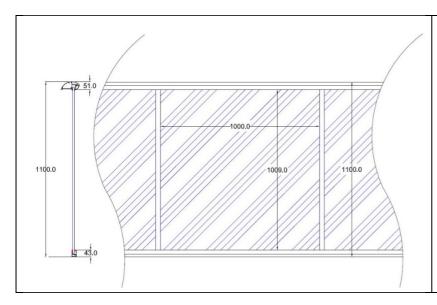
Ultimate moment capacity M_u $f_{g;d} \times Z$ of glass 1000mm wide x

10mm thick 87.53 N/mm² x 16667mm³ x (10) ⁻⁶ =

1.459 kNm/m



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Glass panels can be any length.

For the purposes of design and checking a nominal glass panel width of 1000mm simply supported between the bottom rail and the handrail has been used.

Two separate design conditions are considered:

Uniformly distributed service load on the infill of 1.0 kN/m²

Cition y distinguited service lea	<u>u on the m</u>	<u>0. 2.0 ki t/</u>		
Ultimate UDL on glass	=	1.0 kN/m ² x 1.5	=	1.5 kN/m ²
Ultimate moment on glass	=	$1.5 \text{ kN/m}^2 \text{ x } (1.0)^2$	=	0.1875 kNm/m
due to UDL on 1.0m span		8		
	=	< 1 459 kNm/m	=	OK

The reaction on the handrail from the UDL on the glass is less than the design horizontal UDL on the handrail. Therefore the design load on the glass is not a critical design case in terms of the handrail.

Service point load of 0.5 kN applied in any position on the glass

Worst case for bending stress occurs when the point load is applied at mid-height of the glass.

Ultimate moment on glass	=	(0.50 kN x 1.5) x 1.0m	=	0.1875 kNm
due to point load		4		

Conservatively, it is assumed that this bending moment is carried by a 300mm wide vertical strip of glass.

Moment capacity of 300mm strip	= =	1.459 kNm x 0.30 > 0.1875 kNm	= =	0.4377 kNm OK
Glass deflection: Inertia of glass 1000 x 10mm	=	1000 x (10) ³ / 12	=	83333mm ⁴
Service load deflection due to a UDL of 1.0 kN/m ²	=	5 x (1000 x 1.0) (1000) ³ 384 x 70 000 x 83333	= =	2.232mm OK
Inertia of glass 300 x 10mm	=	0.03 x 83333mm ⁴	=	25 000 mm ⁴
Service load deflection due a point load of 0.5 kN at mid-span	=	500 x (1000) ³ 48 x 70 000 x 25 000	= =	5.95mm OK

The glass is adequate in terms of both bending strength and deflection.



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Glass deflection:

Consider service load deflection of the glass due to the design UDL:

Inertia of glass 10mm thick = $\frac{1000 \text{ x} (10)^3}{1000 \text{ m}}$ = 83333 mm⁴

x 1000mm long 12

Service load deflection = $\frac{5 \text{ w L}^4}{384 \text{ E I}}$

on a simply supported = $\frac{5 \times (1000 \times 1.0) (1000)^3}{2 \times (1000 \times 1.0) (1000)^3}$ = 2.232 mm

span of 1.0m 384 x 70 000 x 83333

< <u>span</u> = OK

65

Conservatively, for deflection calculation purposes consider that the design point load is carried by a 300mm wide vertical strip of glass:

Inertia of glass 10mm thick = $0.3 \times 83333 \text{ mm}^4$ = $25 000 \text{ mm}^4$

x 300mm long

Service load deflection = $\frac{P L^3}{48 E I}$ due to a point load of 0.5 kN 48 E I

applied at mid-span = $500 \times (1000)^3$

48 x 70 000 x 25 000

= 5.95mm

< <u>span</u> = OK

65

The glass is adequate in terms of both bending strength and deflection.

Handrail – bracket connection:

The handrail is connected to the wall brackets by means of 2 No. 4.8mm diameter stainless steel self-tapping screws.

The maximum opening size (and therefore maximum loaded length of handrail) is 3.84m.

Horizontal service (working) = 0.74 kN/m x 1.92mload on the wall fixing for a = 1.421 kN/fixing

clear opening width of 3.84m

Working load shear force = 1.421 kN/2 = 0.71 kN/bolt or screw

on the 4.8mm x 19mm stainless

steel self-tapping screws

Ultimate load shear force on = 0.71 kN/bolt x 1.5 = 1.065 kN/bolt or screw

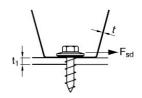
the anchor bolts and screws



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Shearing force, construction screws

Dimensioning value F_{sd} kN/screw. Attention is paid both to failure of the edge of the hole and shearing failure in the screw. Safety class 1.



Nom t mm	When calculating	Tensile yield limit		ew diameter 4_2 mm		Screw diameter 4.8 mm		Screw diameter 5,5 mm			Screw diameter 6,3 mm						
	t mm	N/mm²	t, =t	t ₁ = 2.5 t	t1	t1 =t		t ₁ = 2.5 t		t ₁ = 2.5 t t ₁ = t		t ₁ = 2.5 t		t, =t		t ₁ = 2.5 t	
0.4	0.32	250	0.26	0.54	0.	28	0.	61	0.	30	0.	70	0.	32	0.81		
0.5	0.41	250	0.38	0.69	0.	0.40		0.79		0.43		90	0.	46	1.03		
0.6	0.52	250	0.52	0.86	0.	0.56		0.98		0.60		0.60 1.12		12	0.	64	1.29
0.7	0.60	350	0.93	1.41	1.0	1.00		1.61		1.61 1.07		1.07 1.85		1.	14	2.12	
8.0	0.73	350	1.25	1.72	1.3	1.34		1.96		1.96 1.43		1.43 2.25		1.	53	2,58	
1.0	0.93	250	1.29	1.56	1.3	38	1.79		1.	47	2.	05	1.	58	2,34		
1,0	0,93	350	1,80	2,19	1.5	93	2,50		2,50 2,06		2.	86	2.	21	3,28		
1,2	1,13	350	2,41	2,66	2.	2,58 3,04		2,76		3.	48	2.	95	3,99			
1.5	1.42	250	2,39	2,39	2.	2,60		2,73 2,78		2,78 3,12		2.	97	3,58			
1.5	1,42	350	3,03*	3,03*	3.	3,63		3,64	3,	89	4.	37	4.	16	5,01		
2.0	1.91	350	3.03*	3.03*	4.16	3.64	4.16	3.64	5.72	5.20	5.72	5.20	6.	49	6.74		
2.5	2.40	350	3.03*	3.03*	4.16	3.64	4.16	3.64	5.72	5.20	5.72	5.20	7.80	6.76	7.80 6.76		

In the area of number pairs in the table and marked *, shearing failure in the screw is decisive.

The value to the left in each number pair relates to carbon steel screws, while the number to the right relates to stainless steel screws.

Excerpt of the table at the foot of page 7 of Lindab's literature headed 'Shearing force, construction screws'

Properties of stainless steel self-tapping screws:

material type = stainless steel grade 304

Characteristic ultimate tensile strength = 621 N/mm² Characteristic 0.2% proof stress = 290 N/mm²

Phillips self-tapping screws: ultimate shear loads taken from the table in Lindab's technical literature.

Thickness of aluminium in the = 5.4mm

handrail at screw positions

Ultimate shear capacity of 4.8mm = 3.64 kN/screw (from Lindab's table)

diameter screws, safety class 1

for Nom t = 2.5mm

For safety classes 2 and 3 this value is divided by 1.1 and 1.2 respectively. Safety class 3 is the highest safety class and has been assumed to apply to balustrades. The shear capacities given in Lindab's table are based upon material having a tensile yield limit of 350 N/mm². The values given in the table have been adjusted to allow for the yield stress of stainless steel type 304 (290 N/mm².) The ultimate shear capacity of 3.64 kN/screw has therefore been reduced by 290/350 and divided by 1.2 to represent safety class 3 and 290 N/mm² yield stress rather than 350 N/mm². The adjusted ultimate shear capacity is then 2.51 kN/screw. Exceeds 1.065 kN/screw and therefore OK



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SUMMARY

Juliet balconies using BALCONY 2 System (Aerofoil) handrail with 58 x 4mm steel internal reinforcing bar

- 1. The Juliet Balconette system, comprising Balcony 2 type handrail (with bar) and bottom rail (no bar) in extruded aluminium grade 6063 T5, in conjunction with 10mm thick toughened glass panels, is adequate to support the imposed loads specified in relevant British and European standards in respect of the occupancy classes listed on page 2, for spans up to **4.02 metres** between the centres of handrail support brackets.
- 2. The handrail support brackets in extruded aluminium grade 6063 T5 are adequate to support the specified loads for spans up to **4.02 metres** between handrail bracket centres. The bottom rail brackets in extruded aluminium grade 6063 T5 are adequate at up to **500mm** nominal centres between the brackets.
- 3. For the design loading and 4.02 maximum span between handrail bracket centres, the calculated working load direct pull-out force on each of the top 2 No. bolts on the handrail bracket fixing bolts is **2.78 kN**. For smaller width openings the working load direct pull-out force on the top 2 No. bolts on the handrail brackets are reduced, as listed below:

Handrail length	Opening size	Working load tension on each upper bolt
		(including 50% increase recommended in BS 6180)
1280mm	1020mm	0.74 kN
1500mm	1240mm	0.90 kN
1680mm	1420mm	1.03 kN
1860mm	1600mm	1.16 kN
2180mm	1920mm	1.39 kN
2450mm	2190mm	1.58 kN
2840mm	2580mm	1.86 kN
3200mm	2940mm	2.12 kN

- 4. For bottom rail brackets installed at 500mm nominal centres, the calculated working load direct pull-out force on the top bolt is 0.36 kN, including the 50% increase recommended in BS 6180. The calculated working load shear force on each of the 2 No. fixing bolts 0.09 kN/bolt.
- 5. The installers should satisfy themselves that the fixing bolts chosen are suitable to resist the loads specified in items 3 and 4 above, and also that the structure into which they are to be installed can support these loads.
- 6. The 10mm thick thermally toughened safety glass panels are adequate to support the design loads specified in the relevant British and European Standards.
- 7. The 4.8mm diameter self-tapping stainless steel screws connecting the handrail to the aluminium wall brackets are adequate to support the design loads specified in relevant British and European Standards.

Prepared for and on behalf of Balconette by A G Bice CEng FICE FIStructE